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dmytro_bodnar@hotmail.com, maria.bubnyak@gmail.com

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$$1 + \prod_{n=1}^{\infty} \frac{a_n}{b_n} = 1 + \frac{a_1}{b_1 + \frac{a_2}{b_2 + \dots}}, \quad (1)$$

$$a_n, b_n \quad (n \geq 1) \text{ ó } \quad , \quad k- \quad , \quad a_{kn+p} = a_p, \\ b_{kn+p} = b_p \quad (n = 0, 1, \dots; p = \overline{1, k}).$$

XIX. E. Galios, T. Thiele, A. Pringsheim. O. Perron [12],
H. Wall [13], W. Jones, W. Thron [7].
1966. ().

$$1 + \sum_{k=1}^{\infty} D \sum_{i_k=1}^N \frac{a_{i(k)}}{b_{i(k)}} = 1 + \sum_{i_1=1}^N \frac{a_{i(1)}}{b_{i(1)} + \sum_{i_2=1}^N \frac{a_{i(2)}}{b_{i(2)}} + \dots}, \quad (2)$$

$$a_{i(k)}, b_{i(k)} \in \mathbb{R}, i(k) = i_1, i_2, \dots, i_k \in \{1, 2, \dots, N\}, 1 \leq i_k \leq N, k \geq 1, N \in \mathbb{N} \quad [10].$$

[6], [9], [8], [5],

$$1 + D \sum_{k=1}^{\infty} \frac{a_{i(k)}}{1} = 1 + \sum_{i_1=1}^{i_0} \frac{a_{i(1)}}{1 + \sum_{i_2=1}^{i_1} \frac{a_{i(2)}}{1 + \dots}}, \quad (3)$$

$$a_{i(k)} \in \mathbb{R}, \quad i(k) = i_1, i_2, \dots, i_k, \quad 1 \leq i_k \leq i_{k-1}, \quad k \geq 1, \quad i_0 = N. \quad (3)$$

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$$\left(1 + D \sum_{k=1}^{\infty} \frac{c_{i_k}}{1}\right)^{-1}, \quad (4)$$

$c_{i_k} \neq 0$ ó , $1 \leq i_k \leq i_{k-1}$, $k \geq 1$, $i_0 = N$.

(3)

1.

$a_{i(k)}$

(3)

:

$$P_{i(k),\varepsilon}(\gamma) = P_{i_k,\varepsilon}(\gamma) = \left\{ \omega \in C : |\omega| - \operatorname{Re}(\omega e^{-i\gamma}) \leq 2p_{i_k}(1 - \varepsilon) \cos^2 \gamma/2 \right\},$$

$-\pi < \gamma < \pi$, ε ó , , $(0 < \varepsilon < 1)$, $1 \leq i_k \leq i_{k-1}$, $i_0 = N$

$$p_{i_k} = \frac{1}{2N} \left(1 - \frac{i_k}{2N} \right). \quad (5)$$

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2)

(3)

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a)

k ,

$$a_{i(k)} = 0 \quad (i_p = \overline{1, i_{p-1}}, \quad p = \overline{1, k}),$$

b)

$$\sum_{k=1}^{\infty} \min \left(|a_{i(k)}|^{-1}; i_p = \overline{1, i_{p-1}}, p = \overline{1, k} \right), \quad i(k),$$

$$a_{i(k)} = 0$$

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3)

(3)

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$$K(\gamma) = \left\{ z \in C : \left| z - \frac{e^{-i\gamma/2}}{\cos \gamma/2} \right| \leq \frac{1}{\cos \gamma/2} \right\}. \quad (6)$$

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(2).

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$$V_{i(k)} = V = \left\{ \omega \in C : \operatorname{Re}(\omega e^{-i\gamma/2}) \geq -\frac{1}{2N} \cos \gamma/2 \right\}$$

$$E_{i(k)} = E_{i_k} = \left\{ \omega \in C : |\omega| - \operatorname{Re}(\omega e^{-i\gamma}) \leq 2p_{i_k} \cos^2 \gamma/2 \right\},$$

$1 \leq i_k \leq i_{k-1}$, $i_0 = N$, $k \geq 1$, $-\pi < \gamma < \pi$, p_{i_k}

(5).

(4)

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(4)

2.

$$: c_{i_k} \in P_{i_k}(\gamma),$$

$$P_{i_k}(\gamma) = \left\{ \omega \in C : |\omega| - \operatorname{Re}(\omega e^{-i\gamma}) \leq 2p_{i_k} \cos^2 \gamma/2 \right\},$$

$-\pi < \gamma < \pi$, $i_k = \overline{1, N}$, p_{i_k} (5).

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(4)

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2)

(4)

$K(\gamma)$,

(6).

$$\left(1 + D \sum_{k=1}^{\infty} \frac{z_{i_k}}{1} \right)^{-1}. \quad (7)$$

$$G_2 = G_2(c_1) = \bigcup_{\gamma \in [\gamma_1^1, \gamma_2^1]} P_2(\gamma).$$

$$c_2 \in G_2.$$

$$c_3. \quad c_2 \in P_2(\gamma), \quad \gamma \in [\gamma_1^2, \gamma_2^2],$$

$$\gamma_1^2 = \gamma_1 \quad \gamma_2^2 = \gamma_2.$$

$$(10),$$

$$\gamma_1 \quad \gamma_2$$

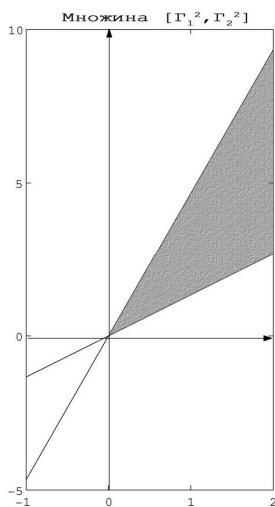
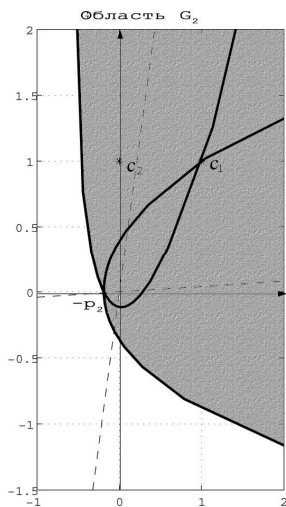
$$a = c_2$$

$$p = p_2.$$

$$(9)-$$

$$[\Gamma_1^2, \Gamma_2^2] = [\gamma_1^1, \gamma_2^1] \cap [\gamma_1^2, \gamma_2^2]$$

$$G_3 = G_3(c_1, c_2) = \bigcup_{\gamma \in [\Gamma_1^2, \Gamma_2^2]} P_3(\gamma).$$



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$$[\Gamma_1^2, \Gamma_2^2]$$

$$G_2$$

$$G_3.$$

$$c_2,$$

$$c_1 = 1 + i.$$

$$c_2 = i.$$

$$(4),$$

$$G_1, G_2, \dots, G_{s-1}$$

$$c_1, c_2, \dots, c_{s-1}$$

$$.$$

$$[\Gamma_1^{s-1}, \Gamma_2^{s-1}] = \bigcap_{j=1}^{s-1} [\gamma_1^j, \gamma_2^j] \quad (12)$$

$$G_s = G_s(c_1, c_2, \dots, c_{s-1}) = \bigcup_{\gamma \in [\Gamma_1^{s-1}, \Gamma_2^{s-1}]} P_s(\gamma) \quad (s = \overline{2, N}). \quad (13)$$

$$,$$

$$G_s$$

$$c_s$$

$$,$$

$$c_s \in P_s(\gamma) \quad \Gamma_1^N \leq \gamma \leq \Gamma_2^N, \quad s = \overline{1, N}.$$

$$3.$$

$$(4)$$

$$:$$

$$c_s \in G_s \quad (s = \overline{1, N}), \quad G_1$$

$$(11),$$

$$G_s(c_1, c_2, \dots, c_{s-1}) \text{ ó}$$

$$(12)- \quad (13) \quad s = \overline{2, N}.$$

$$1)$$

$$(4) \text{ ó}$$

$$;$$

$$2)$$

$$K(\Gamma_1^N) \cup K(\Gamma_2^N), \quad K(\gamma)$$

$$(6), \quad \Gamma_1^N, \Gamma_2^N \text{ ó}$$

$$(12).$$

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$$(13), \quad G_k \neq \emptyset \quad [\Gamma_1^N, \Gamma_2^N] \neq \emptyset.$$

$$\gamma \in [\Gamma_1^N, \Gamma_2^N] : c_k \in P_k(\gamma) \quad (k = \overline{1, N}). \quad 2$$

(4)

 $K(\gamma)$

$$c_k \in P_k(\gamma),$$

$$\Gamma_1^N \leq \gamma \leq \Gamma_2^N,$$

$$K(\Gamma_1^N) \cup K(\Gamma_2^N), \quad K(\gamma) \quad (6).$$

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